

DISCONTINUOUS GALERKIN METHOD FOR THE STOKES EQUATIONS WITH MIXED BOUNDARY CONDITIONS

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ABSTRACT. We propose and analyze a discontinuous Galerkin approximation for the incompressible Stokes problem in two dimension spaces. We suppose that the boundary is divided into three open and disjoint subsets Γ_1 , Γ_2 and Γ_3 . The boundary conditions are mixed with the vorticity condition: $\text{curl } \mathbf{u} = w_0$ and $\mathbf{u} \cdot \mathbf{n} = \mathbf{b} \cdot \mathbf{n} =$ on the first part of the boundary Γ_1 , a pressure condition: $p = p_0$ and $\mathbf{u} \cdot \mathbf{t} = \mathbf{a} \cdot \mathbf{t}$ on Γ_2 and a Dirichlet boundary condition $\mathbf{u} = \mathbf{u}_0$ on Γ_3 . We establish a priori error estimates in the energy norms and we present an a posteriori error estimator of residual type.

Keywords: Discontinuous Galerkin method , Stokes equations, a priori error, a posteriori error

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