

CONSERVATIVE HIGH ORDER COUPLED MIXED FINITE ELEMENT-FINITE VOLUME METHOD FOR TWO-PHASE FLOWS IN HETEROGENEOUS MEDIA

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ABSTRACT. Mass conservation is a crucial requirement of effective computational models for multi-phase flows in heterogeneous porous media [3]. We present a conservative method where Darcy's equation is resolved by the mixed finite element formulation, using hierarchical high order $\mathbf{H}(\text{div})$ -conforming approximation spaces, as described in [2], and the transport of components is updated by means of a second order finite volume scheme [5] based on reconstruction and limitation of gradients. The nonlinear coupled system given by the weighted pressure formulation [4] is implemented in the multiphysics object-oriented scientific computational environment NeoPZ [1]. This is a general finite element approximation software incorporating a variety of element geometries, variational formulations, approximation spaces (e.g. continuous, discontinuous, $\mathbf{H}(\text{div})$, and others), allowing robust implementations of different type of formulations and approximation spaces in a same simulation, including *hp*-adaptivity.

Keywords: finite elements, finite volume, multiphysics simulations, $\mathbf{H}(\text{div})$ spaces, high order methods

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