

UNIVERSIDAD DE CONCEPCION
DIRECCION DE POSTGRADO
CONCEPCION-CHILE



METODO DE ELEMENTOS FINITOS ADAPTATIVOS Y MULTIESCALA
APLICADOS A PROBLEMAS DE MECANICA DE FLUIDOS

*Tesis para optar al grado de
Doctor en Ciencias Aplicadas con mención en Ingeniería Matemática*

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2011

Contents

1	Introducción	1
2	On a hierarchical error estimator combined with a stabilized method for the Navier–Stokes equations	9
2.1	Introduction	9
2.1.1	Notations and Definitions	11
2.2	Model problem	12
2.3	The Stabilized Method	14
2.4	An a posteriori error estimate	17
2.4.1	Preliminary results	17
2.4.2	The auxiliary problem	18
2.4.3	The hierarchical error estimator	24
2.5	Numerical experiments	28
2.5.1	An analytical solution	29
2.5.2	The lid–driven cavity problem	35
3	Convergence Analysis of a Residual Local Projection Finite Element Method for the Navier–Stokes equations	41
3.1	Introduction	41
3.1.1	Notations and preliminaries	43
3.2	The residual local projection method	45
3.3	Error analysis	47

3.3.1	Technical Preliminaries	49
3.3.2	Existence of a discrete solution	51
3.3.3	A priori error analysis	56
3.4	A divergence-free discrete velocity.	68
3.5	Numerical validations	69
3.5.1	A study of convergence	69
3.5.2	The lid-driven cavity flow	72
3.6	Conclusion	73
4	An adaptive Residual Local Projection finite element method for the Navier–Stokes equations	75
4.1	Introduction	75
4.2	Model problem and Preliminary results	77
4.3	The residual local projection method	81
4.4	A residual error estimator	85
4.5	Numerical validation	93
4.5.1	Examples	95
5	Conclusiones y trabajo futuro	121
5.1	Conclusiones	121
5.2	Trabajo futuro	122
A	The discrete Stokes operator	125