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Motherboard heat dissipation design using the Parareal method in PETSc

Benjamín Barán *

Abstract

This work presents a parallel implementation of the Parareal method using PETSc (Portable, Extensible Toolkit for Scientific Computation) to solve a typical motherboard heat dissipation design problem that can be viewed as a parabolic partial differential equation with known boundary conditions and initial state, where the minimized cost function relates the controller energy usage and the approximation of the solution to an optimal known function. The equations that model the process are discretized with Finite Elements in space and Finite Differences in time. After discretization in space and time, the problem is transformed to a huge linear system of algebraic equations that is solved by the Conjugate Gradient method. The Parareal preconditioner is implemented to speed up the convergence of the Conjugate Gradient. The main advantage in using the Parareal method in this parallel implementation in PETSc is to speed up the resolution time, when comparing to implementations that only use the Conjugate Gradient or GMRES methods. The implementation developed in this work offers a parallelization relative efficiency for the strong scaling that is approximately 70\% each time the process count doubles, while for the weak scaling it is 75% each time the process count doubles for a constant solution size per process and up to 96% each time the process count doubles for a constant data size per process.

Key words: motherboard design, parallel implementation in PETSc, Pararreal preconditioner, Finite Elements in space and Finite Difference in time, parallelization efficiency.

References

[1] JUAN J. CÁCERES, BENJAMÍN BARÁN and CHRISTIAN SCHAERER. Implementation of a distributed parallel in time scheme with portable extensible toolkit for scientific computation. 7th Workshop on Computer Aspects of Numerical Algorithms - CANA'14 at the Federated Conference on Computer Science and Information Systems (FedCSIS). Varsovia - Polonia, 2014.

^{*}East National University (UNE) and National University of Asuncion (UNA) - Paraguay. Email: bbaran@pol.una.py

- [2] JUAN J. CÁCERES, BENJAMÍN BARÁN and CHRISTIAN SCHAERER. Solving a parallel in time parabolic differential control problem with PETSc. Conference on Computational Interdisciplinary Science CCIS'2014. Asunción Paraguay, 2014.
- [3] SATISH BALAY, WILLIAM D. GROPP, LOIS CURFMAN McInnes, and Barry F. Smith. Efficient management of parallelism in object oriented numerical software libraries. In E. Arge, A. M. Bruaset, and H. P. Langtangen, editors, Modern Software Tools in Scientific Computing. 163-202. Birkhauser Press, 1997.
- [4] XIUHONG DU, MARCUS SARKIS, CHRISTIAN SCHAERER, and DANIEL SZYLD. Inexact and truncated parareal-in-time Krylov subspace methods for parabolic optimal control problems. Electronic Transactions on Numerical Analysis. 40 (2013), 36-57.
- [5] ROBERT D. FALGOUT and ULRIKE MEIER YANG. hypre: a library of high performance preconditioners. Numerical Solution of Partial Differential Equations on Parallel Computers, 2002.
- [6] JEAN GALLIER. The Schur Complement and Symmetric Positive Semidefinite (and Definite) Matrices. Penn Engineering, 2010.
- [7] JOHN L. GUSTAFSON. Reevaluating Amdahl's Law. Communications of the ACM, 1988.
- [8] Christian E. Schaerer and Eugenius Kaszkurewicz. The shooting method for the solution of ordinary differential equations: A control-theoretical perspective. International Journal of Systems Science. 32(8) (2001), 1047-1053.
- [9] Christian E. Schaerer, Eugenius Kaszkurewicz, and Norberto Mangiavac-Chi. A multilevel schwarz shooting method for the solution of the Poisson equation in two dimensional incompressible flow simulations. Applied Mathematics and Computation. 153(3) (2004), 803-831.
- [10] G. Strang. Introduction to Linear Algebra. Wellesley-Cambridge Press, 1998.
- [11] FUZHEN ZHANG. The Schur Complement and Its Applications, Springer, 2005.